

## Residues

Sep 2024

1. Show that the language  $L = \{(\mathbf{ab})^q \mathbf{c}^p \mid q > p\}$  has infinitely many residues and is therefore not regular.
2. Let  $\Sigma = \{\mathbf{a}, \mathbf{b}\}$ . Consider the language  $L$  of strings where the number of  $\mathbf{a}$ 's is a multiple of 3.
  - (a) List the residues of  $L$  (you may describe residues informally).
  - (b) Using the residues, construct the minimal automaton that accepts  $L$ .