Fixing Letrec (reloaded)

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Abstract

The Revised⁶ Report on Scheme introduces three fundamental changes involving Scheme's recursive variable binding constructs. First, it standardizes the sequential recursive binding construct, letrec*, which evaluates its initialization expressions in a strict leftto-right order. Second, it specifies that internal and library definitions have letrec* semantics. Third, it prohibits programs from invoking the continuation of a letrec or letrec* init expression more than once. The first two changes increase the incentive for handling letrec* efficiently, while the third change gives the compiler more options for transforming letrec and letrec* expressions.

This paper extends an earlier effort of Waddell, Sarkar, and Dybvig to handle the Revised⁵ Report letrec and the (then nonstandard) letrec* efficiently. It presents more aggressive transformations for letrec and letrec* that take advantage of the new prohibition on invoking the continuations of initialization expressions multiple times. The implementation employs Tarjan's algorithm for finding strongly connected components in a graph that encodes the dependencies among the bindings.

Keywords Scheme, recursive binding construct, internal definitions, mutual recursion, mutual definition, continuations, optimization, letrec

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1. Introduction

Scheme's letrec form, used to create recursive bindings, is easily transformed into a standard combination of let and set! expressions [4]. Unfortunately, the standard transformation introduces unnecessary assignments that may inhibit subsequent optimization of the form. An alternative transformation is described by Waddell, Sarkar, and Dybvig [9]. This transformation often succeeds in avoiding unnecessary assignments while maintaining the Revised⁵ Report semantics for letrec. Waddell, et al., also define a variant of letrec, called letrec* by analogy to let*, that evaluates its initialization expressions from left to right, and they present a similar optimizing transformation for letrec*.

The Revised⁶ Report on Scheme [5] changes the status quo by including letrec* as well as letrec in the language and, more importantly, by changing the semantics of internal defines so that define-bound variables behave as if bound by letrec* rather than letrec. An immediate consequence of this changes is that R⁶RS programs (on average) will contain more variables bound according to the letrec* semantics. Thus, optimizing letrec* has become even more important. Over time, we also expect programmers to take advantage of this change by using the values of earlier bindings for the purpose of initializing subsequent ones. Unfortunately, this will result in more of the so-called *complex* bindings for which the Waddell, et al., transformation, like the naive transformation, often produces unnecessary assignments.

The Revised⁶ Report makes one other semantic change in its recursive binding constructs, which is to prohibit programs from invoking the continuation of a letrec or letrec* init expression more than once. This gives the implementation more flexibility to avoid producing assignments whose absence could otherwise

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have been detected by invoking the continuation of an initialization expression multiple times.

This paper presents a new transformation algorithm that often produces fewer assignments than the Waddell, et al., transformation, especially for letrec*. At worst, it produces the same number of assignments as the Waddell, et al., transformation. It accomplishes this by an aggressive partitioning of bindings into minimal mutually dependent groups, aided by Tarjan's algorithm [6] for finding strongly connected components, and by taking advantage of the new prohibition against invoking the continuations of initialization expressions multiple times.

The rest of this paper is organized as follows. Section 2 gives an overview of the syntax and semantics of Scheme's letrec and letrec* forms along with the run-time restrictions imposed by the standard. Section 3 gives the naive but straightforward implementation of these forms based on source-level macro transformation. Section 4 summarizes the fixing letrec algorithm of Waddell, Sarkar, and Dybvig [9]. Section 5 motivates our work by showing simple examples where the original algorithm yields undesirable results. Section 6 describes the constraints that our transformation must follow, the analysis it requires, and how it encodes the information it needs in a graph form. Section 7 shows how the algorithm uses the strongly connectedcomponents to perform the actual transformation. Finally, Section 8 provides some concluding remarks.

2. Semantics of letrec and letrec*

The syntax of the letrec and letrec* forms are identical, except for the opening keyword:

The lexical scoping rules for letrec and letrec* are the same: all of *vars* are visible in all *init* expressions as well as in the *body* definitions and expressions. For both forms, evaluation proceeds as follows:

- 1. All *vars* are bound to fresh locations.
- 2. The *init* expressions are evaluated and the value of each *init* is assigned to the corresponding *var*.
- 3. The body is evaluated and the values of the last expression are returned.

The two forms differ in the specifics of item 2. For letrec, all *init* expressions are evaluated first, in some

unspecified order, before all bindings are initialized to the computed values. For letrec*, the bindings are initialized sequentially: each *init* is evaluated, and the corresponding *var* is set before the next binding is initialized.

2.1 Restrictions

Although all *vars* are visible in all *init* expressions, the actual evaluation of the *init* expressions must obey additional restrictions. For letrec, each *init* expression must evaluate without referencing or assigning the value of any of the *vars*. During the evaluation of letrec* *init* expressions, however, references and assignments to previously initialized bindings (e.g., ones that appear earlier in the list of bindings) are permitted. The R⁶RS requires that implementations *must* detect and report violations of this restriction [5], though some implementations currently ignore this requirement.

The R^6RS also prohibits programs from invoking the continuation (returning from the evaluation) of an *init* expression. The report specifies that implementation *should* detect and report such violations. Thus, portable programs cannot depend on the implementation's behavior when the program violates this prohibition.

Implementations can enforce both of these restrictions via a source code transformation that inserts additional checks.

A transformation that guards against the first restriction with minimal overhead is described by Waddell, et al. [9]. The transformation works as a pre-pass to the fixing letrec algorithm. It first inserts validity checks amounting to binding one *initialized*? variable per letrec expression, or one per letrec* binding, and inserting validity checks anywhere a possible violation of the restriction might occur. Because these checks are separate from the actual letrec or letrec* bindings, the transformation does not inhibit optimizations involving the bindings. Because it works independently, as a prepass, of the transformation of letrec and letrec* into more primitive forms, it is applicable regardless of the transformation used, whether it be the naive transformation, the one described by Waddell, et al., or the more sophisticated transformation described in this paper.

To enforce the second restriction, an implementation can transform an unchecked letrec or letrec* ex-

pression into a checked one via a simple transformation:

```
(define-syntax checked-letrec
 (syntax-rules ()
  [(_ ([var init] ...) b b* ...)
    (letrec ([var (once init)] ...)
        b b* ...)]))
```

where once is a primitive keyword that behaves according to the following definition:

```
(define-syntax once
 (syntax-rules ()
  [(_ expr)
   (let ([returned? #f])
      (let ([v expr])
         (when returned?
            (assertion-violation ---))
        (set! returned? #t)
        v))]))
```

The once wrapper should be omitted at least for *init* expressions that cannot possibly invoke their continuations multiple times, including constants, lambda expressions, variable references, and applications of most primitives to simple values. An implementation might also attempt to omit the once wrapper for other expressions it can prove do not invoke their continuations multiple times.

The remainder of this paper assumes that all uses of letrec and letrec* are either correct (i.e, do not violate the two restrictions of the report stated above) or that the required checks have already been inserted by a prior transformation.

3. Naive letrec / letrec* transformation

The task of the *fixing letrec* pass of the compiler is to rewrite the general Scheme letrec and letrec* forms into simpler forms that subsequent passes of the compiler can easily handle.

The simplest (and most naive) transformation for letrec* can be achieved at the source level via a simple macro:

```
(define-syntax letrec*
  (syntax-rules ()
    [(_ ([var init] ...) b b* ...)
        (let ([var #f] ...)
            (set! var init) ...
            (let () b b* ...))]))
```

It is easy to see how the output of this transformation performs the required letrec* evaluation semantics. (It enforces none of the restrictions, but we are assuming these are enforced by some earlier transformation.) The same transformation can be used for letrec expressions, but it unnecessarily forces the initialization expressions to be evaluated from left to right, preventing the compiler from subsequently choosing a different order that might result in more efficient code. The following definition of letrec avoids specifying a particular evaluation order:

These naive transformations have two unfortunate consequences. First, the compiler cannot always "undo" the transformation since the resulting code overspecifies the intended behavior. That is, the compiler cannot tell whether the resulting code is intended to behave according to the letrec / letrec* semantics, or whether it really means binding some variables to a constant (#f) followed by assigning these variables to some other values. Second, some optimizing compilers of Scheme cannot handle assigned variables as efficiently as unassigned ones. In addition to inhibiting inlining, copy-propagation, constant folding, direct jumps to local procedures, and other optimizations, assigned variables often end up being boxed in heapallocated locations [1], thus introduce additional runtime overhead for heap overflow checks when the bindings are introduced, additional memory traffic when the bindings are used, and possibly additional garbage collection overhead.

4. Waddell's letrec transformation

The Waddell, et al., algorithm for *fixing letrec* works by transforming a letrec expression into a set of let and fix binding forms. The fix binding form is a restricted form of letrec in which all bound *vars* are unassigned and all *inits* are lambda expressions. The transformation partitions the letrec bindings into four sets:

1.	[xu	eu]	•••	unreferenced
2.	[xs	es]	•••	simple
3.	[xl	el]	•••	lambda
4.	[xc	ec]	• • •	complex

Unreferenced bindings are those evaluated for effect only: their computed values are never used in the program. Bindings that are unreferenced in the program are eliminated as are assignments to these unreferenced bindings. The simple bindings are those satisfying the following criteria: (1) the var is unassigned, (2) the init is not a lambda expression and does not contain a reference to any *var* bound in the same letrec, and (3) evaluating its *init* expression cannot capture and invoke its continuation more than once. (In R⁵RS Scheme, an initialization expression is permitted to invoke its continuation more than once, but expressions that do are not considered simple.) The lambda bindings set contains the bindings where the var is unassigned and the *init* is a lambda expression. The *lambda* bindings are bound using fix in the output of the transformation. All other bindings are considered *complex*.

After partitioning the bindings, a letrec expression is transformed to:

with the inner let expression omitted if no bindings are *complex*.

For letrec*, the bindings are similarly partitioned into *unreferenced*, *simple*, *lambda*, and *complex* bindings following the same criteria used for letrec expressions. The only difference in the transformation is that the *unreferenced init* expressions and the assignments to *complex* bindings must be interleaved in order to preserve the left-to-right evaluation order required for letrec*. Assuming no unreferenced bindings, a letrec* expression is transformed to:

```
(let ([xs es] ... ; simple bindings
      [xc #f] ...) ; complex bindings
 (fix ([xl el] ...) ; lambda bindings
      (set! xc ec) ... ; complex inits
      body))
```

Because some expressions considered simple for purposes of the letrec transformation might raise exceptions or perform side effects, the rules for simple expressions given above are too liberal to preserve the strict left-to-right evaluation order constraint for letrec* initialization expression. Thus, the Waddell, et al., transformation treats as *complex* any otherwise simple binding whose right-hand side is not effect free" [9]. For example, the expression (car x) is not considered *simple* for purposes of the letrec* transformation, since the car procedure may raise an exception if x is not a pair. In general, an expression cannot be considered effect free if it modifies state, exits from the program, raises an exception, or might not terminate. This has the unfortunate consequence of making many bindings complex, leading to all the drawbacks of assigned variables mentioned earlier. To be effective, fixing letrec should have a better story for handling such *init* expressions than to treat them as *complex*.

5. Why does it matter?

Consider the following simple program fragment:

```
(let ()
  (define q 8)
  (define f (lambda (x) (+ x q)))
  (define r (f q))
  (define s (+ r (f 2)))
  (define g (lambda () (+ r s)))
  (define t (g))
  t)
```

which should be understood in terms of a straightforward transliteration into letrec*, with the bindings appearing in the same order.

According to the Waddell, et al., partitioning algorithm, the binding for q is considered *simple*, the bindings for f and g are *lambda*, and the bindings for r, s, and t are *complex*. After *fixing letrec*, the code is transformed to:

```
(let ([q 8])
  (let ([r #f] [s #f] [t #f])
      (fix ([f (lambda (x) (+ x q))]
```

```
[g (lambda () (+ r s))])
(set! r (f q))
(set! s (+ r (f 2)))
(set! t (g))
t)))
```

Because the variables q, f, and g are unassigned, they are straightforward targets for inlining, copy propagation, and other optimizations performed by a source optimizer such as the one described by Waddell and Dybvig [7, 8]. The assigned variables r, s, and t are not, so the resulting code after optimization might look like the following less-than-ideal code:

```
(let ([t #f] [s #f] [r #f])
 (set! r 16)
 (set! s (+ 10 r))
 (set! t (+ r s))
 t)
```

Compare this with the following program, which at the source level appears less efficient as it contains several more lambda expressions and procedure calls:

```
(let ()
  (define q (lambda () 8))
  (define f (lambda (x) (+ x (q))))
  (define r (lambda () (f (q))))
  (define s (lambda () (+ (r) (f 2))))
  (define g (lambda () (+ (r) (s))))
  (define t (lambda () (g)))
  (t))
```

It is discomforting and counterintuitive that the Waddell and Dybvig source optimizer boils this down to just the constant "42" while the simpler program shown at the beginning of this section does not, all because the letrec* transformation produces unnecessary assignments.

The goal of an efficient letrec and letrec* transformation is to reduce the number of emitted variable assignments (set!s) by turning as many of the bindings into simple let or fix bindings as possible. The original *fixing letrec* algorithm fails to do so, in essence, because it assumes that all of the bindings are possibly mutually dependent and thus must be grouped together in the output.

The new algorithm removes this restriction by grouping a set of bindings together only if they are mutually dependent. It can thus handle each nonrecursive complex binding in a group by itself without introducing an assignment. For example, it transforms the program given above into the following assignment-free program:

6. Constraints, analysis, and encoding

Ideally, the transformation would place each letrec or letrec* binding in its own let or fix expression, each nested inside the previous ones, and so avoid all assignments. It cannot do so, however, due to semantic constraints that must be obeyed in order to handle the full generality of letrec and letrec*.

6.1 Constraints due to lexical scope

The lexical scope rule for let bindings requires that the right-hand-side expressions cannot reference any of the left-hand-side variables or any variables not bound in an outer scope. So, if x and y are two letrec bindings, we cannot place x in an outer let to y if x's *init* expression refers to y.

The lexical scope rule for fix bindings allows for mutual recursion among lambda expressions: the variables at the left-hand-side can appear at the right-handside lambda expressions as well as in the fix body. Consider the following example:

```
(let ()
  (define f (lambda () (even? 5)))
  (define even?
      (lambda (x)
         (or (zero? x) (odd? (- x 1)))))
  (define odd?
      (lambda (x) (not (even? x))))
  (define t (f))
  t)
```

Because even? and odd? are mutually recursive, they must be bound by the same fix. The procedure f references even?, but neither even? nor odd? references f, so f is placed in an inner fix. (Since it is nonrecursive, it could be bound by let instead, but we bind it using fix to facilitate a later, independent transformation that combines nested fix expressions to simplify the block allocation and wiring together of procedures.) The variable binding t is placed inside the binding for f since it references f, and none of the other bindings reference it. The final product of the transformation shows the effect of scoping constraints on the output of the transformation.

The transformation cannot transform all letrec and letrec* forms into arbitrarily nested let and fix bindings and thus avoid ever producing an assignment. For example, the program

```
(letrec ([x (list (lambda () x))]) x)
```

necessarily requires the introduction of an assignment to establish the cyclic relationship between the procedure and the pair. It is thus transformed into the following equivalent program

```
(let ([x #f])
  (set! x (list (lambda () x)))
  x)
```

Similarly, an assignment may be introduced for more than one recursively defined nonprocedure binding. In the following example, x and y are mutually recursive nonprocedure bindings, both requiring an assignment. The binding for f refers to both x and y but it can appear in an inner binding because neither x nor y refers to it.

```
(let ()
  (define x (list (lambda () y)))
  (define f (lambda () (cons x y)))
  (define y (list (lambda () x)))
  (define t (f))
  t)
=>
(let ([x #f] [y #f])
  (fix ([f (lambda () (cons x y))])
    (set! x (list (lambda () y)))
    (set! y (list (lambda () x)))
    (let ([t (f)])
    t)))
```

If the initialization expressions for two complex bindings are not mutually recursive, however, the assignments can be avoided. For example, assuming x, f, and g are defined outside of the following expression and both y and z are referenced within body:

```
(let ()
  (define y (f x))
  (define z (g x))
  body)
```

is transformed into the following.

This transformation would also be valid for the equivalent letrec expression, with the R^6RS semantics. It would not be valid for internal defines following the R^5RS letrec semantics, however, since a continuation catpured by f might be invoked multiple times, each causing a new location for z to be created, possibly holding a different value each time.

6.2 Constraints due to evaluation order

For letrec* (but not for letrec), an additional constraint on the transformation is forced by the requirement that the *init* expressions be evaluated sequentially from left to right. Evaluating an *init* expression may, however, cause side effects. The letrec* transformation therefore *must* preserve the order of observable side effects in the *init* expressions as they appear in the input program.

Whether an *init* expression causes an observable side effect is undecidable in general, so the analysis to determine whether it does so must be conservative. Our current implementation considers an *init* expression to have a side effect if it contains a procedure call or a set! expression occurring outside of a lambda expression. This gives the implementation the freedom to reorder the simple bindings comprising of constants, variable references, primitive references, lambda expressions, and the combination of simple expressions to form certain primitive calls, if, begin, let, letrec, and letrec* expressions.

6.3 Viewing constraints as a dependency graph

The first part of our algorithm works by encoding each letrec and letrec* instance as a directed graph G

in which the nodes are the set of *vars* and the arcs represent the dependencies between bindings.

The dependencies are derived from the lexical scope and (for letrec*) evaluation order constraints and control the overall structure of the result of the transformation. For example, the lexical scope rule dictates that at the output of the transformation, an *init* in an outer let or fix binding must not reference a variable placed in an inner binding. Or, stated differently, if x_i appears free in some $init_j$ expression, x_i has to be bound before (or at the same time) $init_j$ is evaluated but not later. Thus, the binding for x_j is said to depend on the binding for x_i as in the following definition:

Dependency graph for letrec:

Given a set of bindings $\{\langle x_i, init_i \rangle *\}$, the dependency graph is $G = \langle V, E \rangle$ where $V = \{x_i *\}$ and $E = \{(x_j, x_i) : x_i \in FV(init_j)\}.$

Constraints due to the specified evaluation order for letrec* are encoded in a similar fashion. If two *init* expressions might perform observable side effects, their order must be preserved in the output of the transformation. Thus, the edges of the dependency graph for letrec* must contain an arc $x_j \rightarrow x_i$ if *init*_j must be evaluated after *init*_i.

Dependency graph for letrec*:

Augments the edges of the corresponding letrec graph with the set

 $\{(x_j, x_i) : init_j \text{ and } init_i \text{ are } complex \text{ and } j > i\}.$

Dependencies are transitive, e.g., if $(x_i, x_j) \in E$ and $(x_j, x_k) \in E$, then $(x_i, x_k) \in E$ and thus need not be encoded explicitly. In fact, our implementation adds at most N - 1 order-of-evaluation edges for a letrec* containing N bindings and not the $O(N^2)$ edges required if all pairs of dependent bindings are connected.

The dependency graphs for the programs presented so far are shown in figure 1. It is instructive to compare each dependency graph with the corresponding code after transformation.

6.4 Strongly connected components

Once the dependencies among bindings are determined, the resulting graph is partitioned into strongly



Figure 1. The dependency graphs for the first three source programs shown in Section 6. The left-most graph is for the program at the beginning of Section 5. The two shorter graphs are for 6.1 and 6.2. The edges in these graphs record the constraints due to lexical scope and evaluation order.

connected components (SCCs) using Tarjan's algorithm [6]. An SCC in G is the largest subgraph of G in which every node is reachable when starting from every other node in the SCC.

The Tarjan algorithm works by visiting all reachable nodes starting from some node x_s , in a depth-first-order traversal, ranking each node with its depth of traversal, and combining cycles as they are encountered.

In its simplest case, an SCC contains just a single node (which may or may not be pointing back to itself). If an SCC contains more than one node, these nodes are mutually dependent, either because they are mutually recursive or because one node references another that must follow it in the left-to-right evaluation order of letrec*.

The arcs of G not only determine the set of SCCs but also defines a partial order relation on the SCCs. Our implementation of Tarjan's algorithm returns an ordered list of SCCs such that SCC_i does not depend upon SCC_j if i < j, but SCC_j might depend on SCC_i .

7. Transformation based on SCCs

The letrec and letrec* transformation partitions the set of bindings into strongly connected components.

We only need to consider how to generate code for a single SCC. This is because the list of SCCs obtained from the Tarjan algorithm is ordered according to the required dependencies, so the bindings for each SCC need merely be nested within the bindings for previous SCCs.

Each SCC is handled in a manner similar to the way the Waddell, et al., transformation handles the entire set of letrec and letrec* bindings, except that we treat specially the case where an SCC contains only one binding.

Single bindings: Code generation for an SCC containing a single binding $\langle var, init \rangle$ is handled according to one of the following cases:

- If *init* is a lambda, and *var* is unassigned: (fix ([*var init*]) *rest*)
- If var ∉ FV(init):
 (let ([var init]) rest)
- Otherwise, we resort to assignment: (let ([var #f])

(set! var init) rest)

The *rest* code in the transformation denotes the code for subsequent SCCs and the transformed *body* expression.

Multiple bindings Code generation for an SCC containing multiple bindings is done by partitioning the bindings into two parts:

- 1. $\langle var_{\lambda}, init_{\lambda} \rangle$ if *init* is a lambda expression and *var* is unassigned.
- 2. $\langle var_c, init_c \rangle$ otherwise.

Tarjan's algorithm does not guarantee an order of returned elements for each SCC, so, for letrec*, the complex bindings need to be sorted according to their occurrence in the original letrec* form. The two partitions are used to produce the following code:

```
(let ([var<sub>c</sub> #f] ...)
  (fix ([var<sub>λ</sub> init<sub>λ</sub>] ...)
     (set! var<sub>c</sub> init<sub>c</sub>) ...
     rest))
```

The graphs shown in Figure 1 tell the whole story. The first graph shows a long chain of dependencies, but all SCCs are of size 1. This is why the transformed code

(shown at the end of Section 5) has a deeply nested let and fix forms, each binding a single variable. The second graph (the even?/odd? example) shows two mutually recursive bindings in one SCC (producing a fix binding in the output) and two singleton SCCs (producing two let bindings). The last graph also shows an SCC with two bindings, but this time, x and y cannot be bound with fix, and thus an assignment is needed.

8. Conclusions

The letrec and letrec* transformation algorithm described in this paper improves on the handling of letrec and letrec* by Waddell, et al. [9], by producing fewer assignments, thus reducing direct overhead from assignments as well as the indirect overhead from the inhibition of certain optimizations. Each binding that would be considered *simple* by the Waddell, et al., transformation ends up in its own SCC. Since simple bindings cannot reference any of the left-handside variables, they are handled by the second singlebinding case above, i.e., they are bound by let expressions. Similarly, all lambda bindings end up bound by fix expressions. The difference between the Waddell, et al., transformation and ours is in the treatment of bindings the former considers complex. While the Waddell, et al., transformation always introduces assignments for *complex* bindings, our transformation avoids assignments for those that are nonrecursive and end up in their own SCC, which appears in our initial experiments to be by far the most common case. For letrec*, some apparently *simple* bindings must be considered complex, such as primitive calls that might raise exceptions, so this improvement is particularly important for R⁶RS, which employs letrec* semantics for internal definitions.

We have implemented the original and new algorithms and wired them into the Ikarus [3] and Chez Scheme [2] compilers, with a parameter to select which algorithm to run. Using both systems, we compared the effectiveness of the two algorithms in eliminating complex bindings while bootstrapping the compiler and run-time libraries, which for both systems involves thousands of letrec or letrec* bindings. 10% of Ikarus's bindings and 7.2% of Chez Scheme's bindings are considered complex by the original algorithm versus only .6% and .1% for the new. Thus, in both systems, the complex bindings are a substantial fraction of all letrec/letrec* bindings using the original algorithm, but an insignificant fraction using the new.

Although the bootstrapping times for Ikarus improve by just under 11% when switching from the original to new algorithms, the bootstrapping times for Chez Scheme do not improve significantly. This is likely due, in part, to the fact that most of the code that affects Chez Scheme's compile-time was written before letrec* was introduced and internal definitions were changed to use letrec* semantics. Furthermore, most of the code was developed with an even less effective algorithm for handling letrec than the Waddell, et al., algorithm, and this has caused the developers to shy away from potentially complex bindings in timecritical portions of the system.

Based partly on our experience, we believe that programmers will take advantage of the letrec* semantics for internal definitions, especially with the knowledge that letrec* can be implemented effectively, and that the improvement afforded by the new transformation will become increasingly more valuable over time. It will be interesting to test this hypothesis once a large corpus of programs written specifically for R⁶RS becomes available.

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